Carnegie Mellon University Heinzcollege

94-775/95-865 Lecture 8: Topic Modeling Wrap-up, Introduction to Predictive Data Analytics

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Quiz Results





Mean: 51.7, standard deviation: 16.1

How to Choose Number of Topics k?

Something like CH index is also possible:

numerical

avoid

issues

For a specific topic, look at the *m* most probable words ("top words")

Coherence (within cluster/topic variability):

log $\frac{\text{# documents that contain both } v \text{ and } w + 0.1}{\text{# documents that contain } w}$

top words v,wthat are not the same $\log of P(see word v | see word w)$

Inter-topic similarity (between cluster/topic variability):

Can average Count # top words that do not appear in each of these any of the other topics' *m* top words across the (number of "unique words") topics

Topic Modeling: Last Remarks

- There are actually *many* topic models, not just LDA
 - Correlated topic models, Pachinko allocation, biterm topic models, anchor word topic models, ...

- Dynamic topic models: tracks how topics change over time
 - Example: for text over time, figure out how topics change
 - Example: for recommendation system, figure out how user tastes change over time

Disclaimer: unfortunately "k" means many things

What if we have labels?



Example: MNIST handwritten digits have known labels

If the labels are known...

If the labels are known...

And we assume data generated by GMM...

What are the model parameters?

k = # of colors

We can directly estimate cluster means, covariances

Flashback: Learning a GMM

Don't need this top part if we know the labels!

Step 1: Pick guesses for cluster means and covariances

Repeat until convergence:

Step 0: Pick k

Step 2: Compute probability of each point belonging to each of the k elusters

Step 3: Update **cluster means and covariances** carefully accounting for probabilities of each point belonging to each of the clusters

We don't need to repeat until convergence

If the labels are known...

And we assume data generated by GMM...

What are the model parameters?

k = # of colors

We can directly estimate cluster means, covariances

What should the label of this new point be? Whichever cluster has higher probability! Decision boundary

We just created a **classifier** (a procedure that given a new data point tells us what "class" it belongs to)

This classifier we've created assumes a generative model

What should the label of this new point be? Whichever cluster has higher probability!

You've seen generative models before for prediction

Linear regression!





Predictive Data Analysis

Training data

$$(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$$

Goal: Given new feature vector x, predict label y

- *y* is discrete (such as colors red and blue)
 → prediction method is called a classifier
- *y* is continuous (such as a real number)
 → prediction method is called a regressor
- A giant zoo of methods

Generative Models

- Hypothesize a specific way in which data are generated
- After learning a generative model:
 - We can generate new synthetic data from the model
 - Usually generative models are probabilistic and we can evaluate probabilities for a new data point
- In contrast to generative models, there are *discriminative* methods that just care about learning a prediction rule

Example of a Discriminative Method: *k*-NN Classification

What should the label of this new point be?

1-NN classifier prediction

What should the label of this new point be?





What happens if k = n?

How do we choose k?

What I'll describe next can be used to select hyperparameter(s) for any prediction method

First: How do we assess how good a prediction method is?

Hyperparameters vs. Parameters

- We fit a model's parameters to training data (terminology: we "learn" the parameters)
- We pick values of hyperparameters and they do not get fit to training data
- Example: Gaussian mixture model
 - Hyperparameter: number of clusters *k*
 - Parameters: cluster probabilities, means, covariances
- Example: *k*-NN classification
 - Hyperparameter: number of nearest neighbors *k*
 - Parameters: N/A



Example: Each data point is an email and we know whether it is spam/ham

Example: future emails to classify as spam/ham

Predicted labels

Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point
Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point

Train method on data in gray

Predict on data in orange

Compute prediction error

50%

Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point
Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point

Train method on data in gray

Predict on data in orange

Compute prediction error

0% 50%

Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point
Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point

Train method on data in gray

Predict on data in orange

Compute prediction error

50% 0% 50%

Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point
Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point

Train method on data in grayPredict on data in orangeComputeCompute0%50%0%50%

Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point
Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point

Train method on data in grayPredict on data
in orangeCompute
prediction errorCompute
prediction error0%0%50%Average error: (0+0+50+0+50)/5 = 20%

Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point
Training	Training	Training	Training	Training
data	data	data	data	data
point	point	point	point	point

- 1. Shuffle data and put them into "folds" (5 folds in this example)
- 2. For each fold (which consists of its own train/validation sets):(a) Train on fold's training data, test on fold's validation data(b) Compute prediction error
- 3. Compute average prediction error across the folds

not the same *k* as in *k*-means or *k*-NN classification *k*-fold Cross Validation



- 1. Shuffle data and put them into "folds" (k=5 folds in this example)
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not the same *k* as in *k*-means or *k*-NN classification *k*-fold Cross Validation



- 1. Shuffle data and put them into "folds" (k=5 folds in this example)
- 2. For each fold (which consists of its own train/validation sets):
 (a) Train on fold's training data, test on fold's validation data
 (b) Compute some sort of prediction score
- 3. Compute **average prediction score** across the folds "cross validation score"

Choosing k in k-NN Classification

Note: *k*-NN classifier has a single hyperparameter *k*

For each k = 1, 2, 3, ..., the maximum k you are willing to try:

Compute 5-fold cross validation score using *k*-NN classifier as prediction method

Use whichever k has the best cross validation score

Automatic Hyperparameter Selection

Suppose the prediction algorithm you're using has hyperparameters $\boldsymbol{\theta}$

For each hyperparameter setting θ you are willing to try:

Compute 5-fold cross validation score using your algorithm with hyperparameters θ

Use whichever θ has the best cross validation score Why 5?

People have found using 10 folds or 5 folds to work well in practice but it's just empirical — there's no deep reason

Training data

Training data

Training data

Important: the errors from simple data splitting and cross-validation are *estimates* of the true error on test data!

Example: earlier, we got a cross validation score of 20% error

This is a guess for the error we will get on test data This guess is <u>not</u> always accurate!

Example: Each data point is an email and we know whether it is spam/ham



Cross-Validation Remarks

- *k*-fold cross-validation is a <u>randomized</u> procedure
 - Re-running CV results in different cross-validation scores!
- Suppose there are *n* data points and *k* folds
 - If we are trying 10 different hyperparameter settings, how many models do we fit?
 - If this number is similar in size to *n*, CV can overfit!
 - How many training data are used to train each model during cross-validation?
 - Smaller # folds typically means faster training
- If k = n, would re-running cross-validation result in different cross-validation scores? What about k = 2?

Different Ways to Measure Accuracy

Simplest way:

 Raw error rate: fraction of predicted labels that are wrong (this was in our cross validation example earlier)

In "binary" classification (there are 2 labels such as spam/ham) when 1 label is considered "positive" and the other "negative":

- Precision: among data points predicted to be "positive", what fraction of these predictions is correct?
- **Recall:** among data points that are actually "positive", what fraction of these points is predicted correctly as "positive"? (also called **true positive rate**)
- **F1 score:** 2 × precision × recall

precision + recall